

A few useful Spherical Trigonometry Formulae

As in plane trigonometry the angles of a spherical triangle are referred to as **A**, **B** and **C**, and the sides **a**, **b** and **c** are expressed in angular measure.

$$\cos a = \cos b \times \cos c + \sin b \times \sin c \times \cos A$$

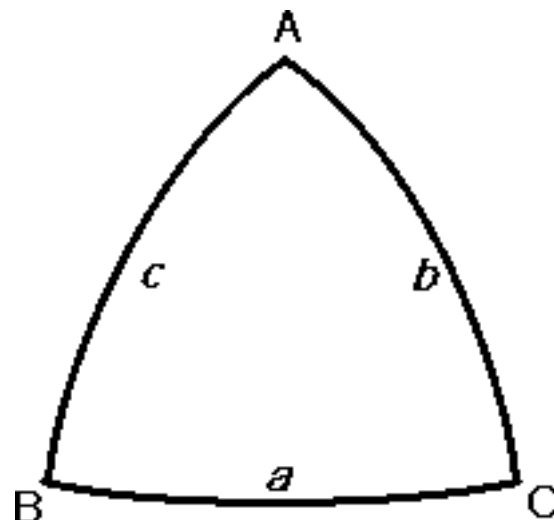
$$\cos b = \cos c \times \cos a + \sin c \times \sin a \times \cos B$$

$$\cos c = \cos a \times \cos b + \sin a \times \sin b \times \cos C$$

$$\cos A = -\cos B \times \cos C + \sin B \times \sin C \times \cos a$$

$$\cos B = -\cos C \times \cos A + \sin C \times \sin A \times \cos b$$

$$\cos C = -\cos A \times \cos B + \sin A \times \sin B \times \cos c$$



In any spherical triangle

$$\frac{\sin a}{\sin A} = \frac{\sin b}{\sin B} = \frac{\sin c}{\sin C}$$

If three sides of a spherical triangle are known then:

$$\text{Hav } A = \text{cosec } b \times \text{cosec } c \times \sqrt{\text{hav } [a + (b - a)] \times \text{hav } [a - (b - c)]}$$

In a **right spherical triangle**, that is with angle **C** being a 90° angle the following hold true:

$$\sin a = \sin A \times \sin c$$

$$\sin b = \sin B \times \sin c$$

$$\tan a = \cos B \times \tan c$$

$$\tan a = \tan A \times \sin b$$

$$\tan b = \cos A \times \tan c$$

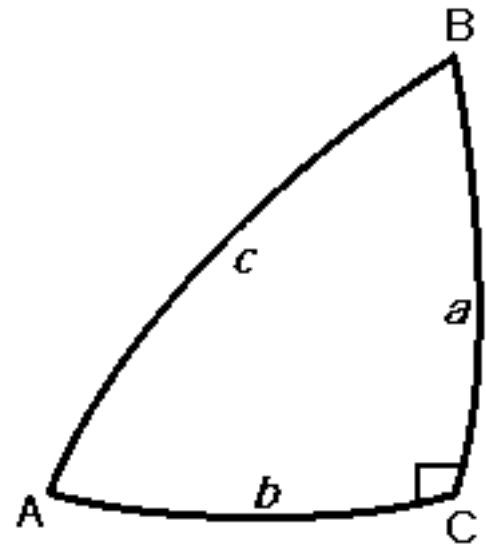
$$\tan b = \tan B \times \sin a$$

$$\cos A = \sin B \times \cos a$$

$$\cos B = \sin A \times \cos b$$

$$\cos c = \cos a \times \cos b$$

$$\cos c = \cot B \times \cot A$$



AREA

The area of a spherical triangle *as measured on the surface of the earth* is:

$$A + B + C - \pi$$

Where **A**, **B**, **C** are expressed in Radians. To convert degrees to radians multiply by $\pi/180$. The answer will be in Radians squared and needs to be multiplied by $(180/\pi * 180/\pi)$ to give square degrees which needs to be multiplied by 3600 to give square nautical miles. Alternately multiply the answer by 11818102.86.

The area of any other spherical triangle is:

$$(A + B + C - \pi) \times R^2$$

Where R, in radians, is the radius of the sphere on which the triangle occurs.

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