

Test statistic used: the mean value of all rolls.

$H_0$  (null hypothesis) is the die is fair because the sample mean does not statistically differ from the expected mean.

$H_a$  (alternate hypothesis) is the die is not fair because the sample mean falls into the critical region.

Outcome	Freq	totals
1	7	7
2	9	18
3	14	42
4	7	28
5	18	90
6	5	30
	avg =	3.583333

Since we're sampling, let's use sampling theory, with a 2 tail test with an  $\alpha = 0.05$ .

We know from our data / experiment the sample mean:

$$n := 60 \quad \mu_{\bar{x}} := 3.58333 \quad s := 1.5436$$

The statistics for a "fair" die follow a discrete uniform distribution AND are KNOWN. Since we know the underlying population standard deviation, we use the z statistic.

$$\bar{x} := \frac{(1 + 2 + 3 + 4 + 5 + 6)}{6} = 3.5 \quad \sigma := \sqrt{\frac{6^2 - 1}{12}} = 1.708$$

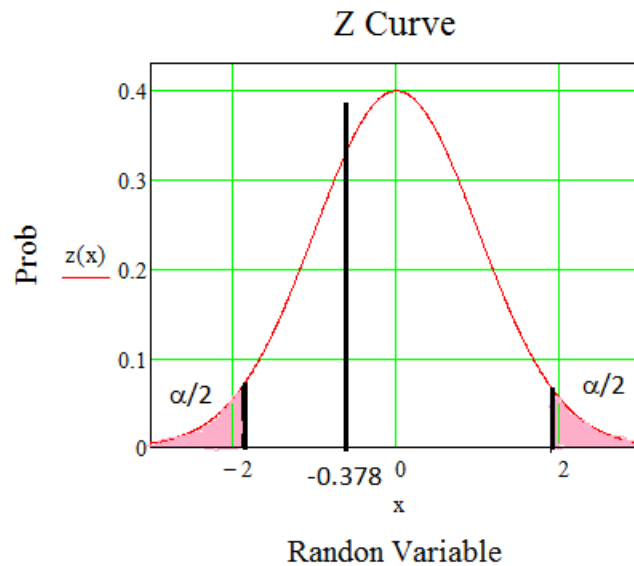
Our z test statistic is:

$$z := \frac{\bar{x} - \mu_{\bar{x}}}{\frac{\sigma}{\sqrt{n}}} = -0.378$$

$$z(x) := \text{dnorm}(x, 0, 1)$$

We know from the Z Chart that critical value = -1.96. The test statistic falls far short of entering the critical region!

Since the probability of the test statistic **does not** fall into the critical region ( $p > 0.975$  or  $p < 0.025$ ), the Null Hypothesis ( $H_0$ ) that the die is fair) **is NOT rejected**.



**We have no reason to reject  $H_0$  (the null hypothesis stating that the die is FAIR).**

**WE MAKE NO ADDITIONAL statements! We would NEVER say "The die is fair."**